Hough Transform

- General idea: transform from image coordinates to parameter space of feature
  - Need parameterized model of features
  - For each pixel, determine all parameter values that might have given rise to that pixel; vote
  - At end, look for peaks in parameter space

From Szymon Rusinkiewicz, Princeton

Hough Transform for Lines

- Generic line: $y = ax+b$
- Parameters: a and b

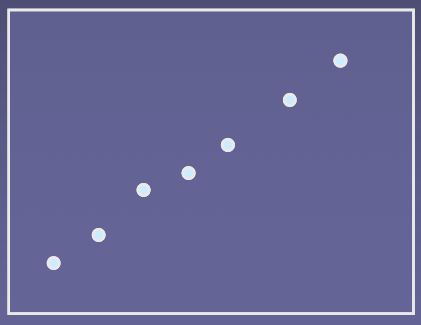
From Szymon Rusinkiewicz, Princeton

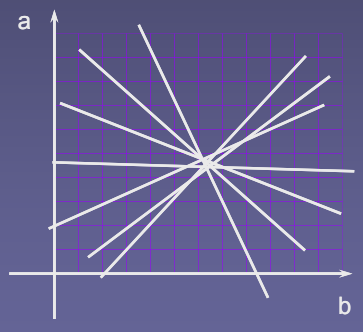
Hough Transform for Lines

1. Initialize table of *buckets*, indexed by *a* and *b*, to zero
2. For each detected edge pixel (*x*,*y*):
   a. Determine all (*a*,*b*) such that $y = ax+b$
   b. Increment bucket (*a*,*b*)
3. Buckets with many votes indicate probable lines

From Szymon Rusinkiewicz, Princeton

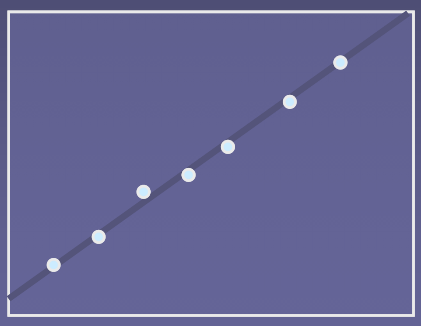
Hough Transform for Lines

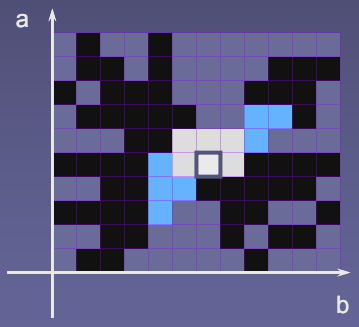




From Szymon Rusinkiewicz, Princeton

Hough Transform for Lines

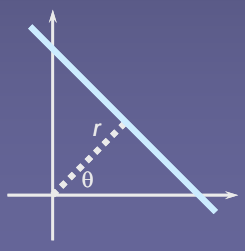




From Szymon Rusinkiewicz, Princeton

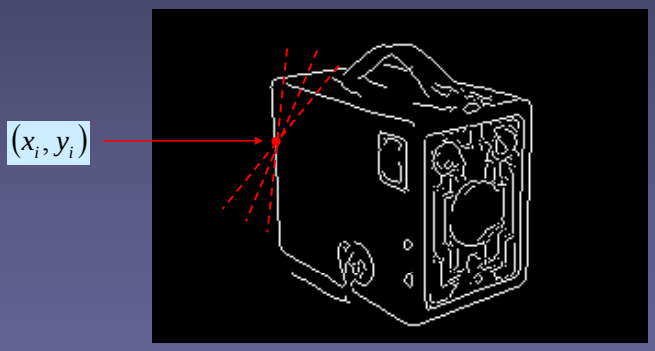
Difficulties with Hough Transform for Lines

- Slope / intercept parameterization not ideal
  - Non-uniform sampling of directions
  - Can't represent vertical lines
- Angle / distance parameterization
  - Line represented as (r,θ) where $x \cos \theta + y \sin \theta = r$



From Szymon Rusinkiewicz, Princeton

Finding Lines Using the Hough Transform

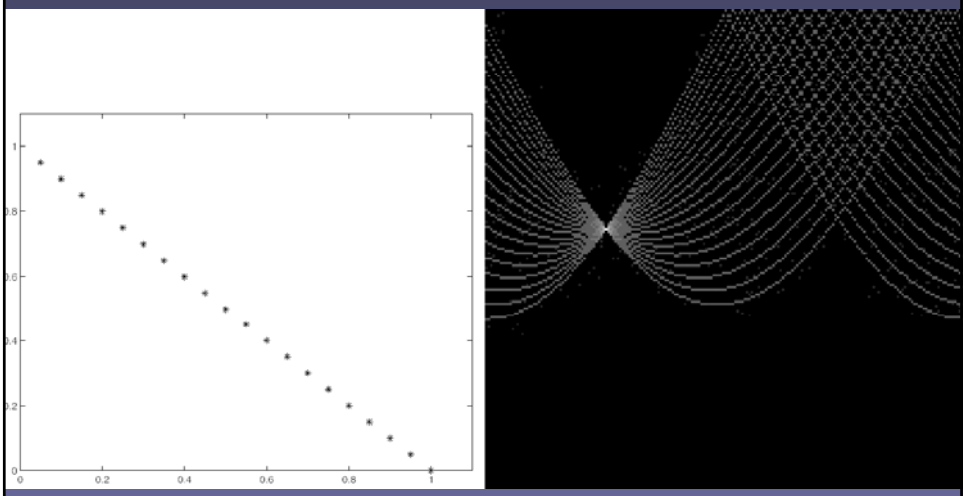


$$\rho = x_i \cos\theta + y_i \sin\theta$$

Algorithm

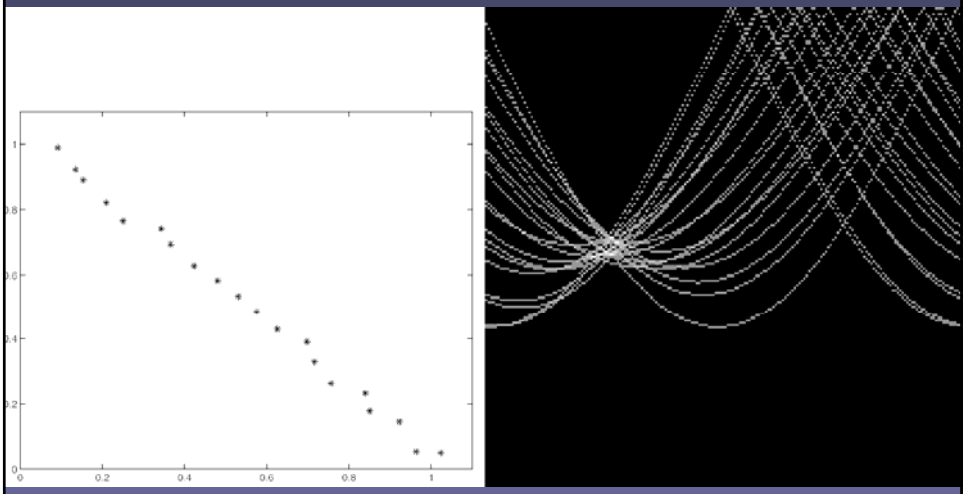
- Discretize the parameter spaces ρ and θ.
- Create Accumulator array A(1..R,1..T).
- Set A(k,h)=0 for all k and h.
- For each image edge E(i,j)=1
  - For h=1…T
    - $\rho = i \cos\theta_d(h) + j \sin\theta_d(h)$
    - Find index k: ρ_d is closest to ρ
    - Increment A(h,k) by one.
- Find all local maxima (k_p, h_p) such that $A(k_p, h_p) > \tau$

Hough Transform Results



Forsyth & Ponce

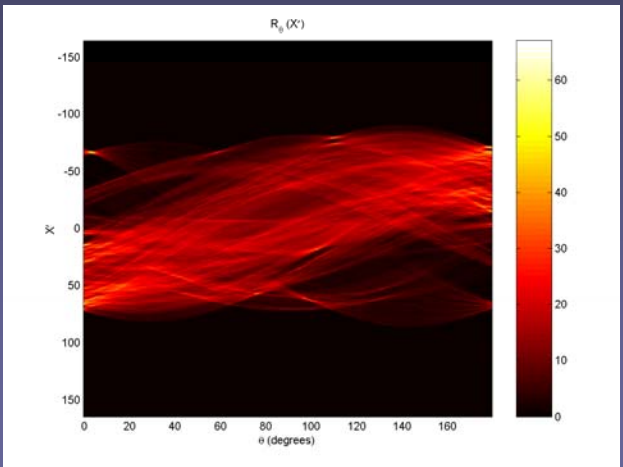
Hough Transform Results



Forsyth & Ponce

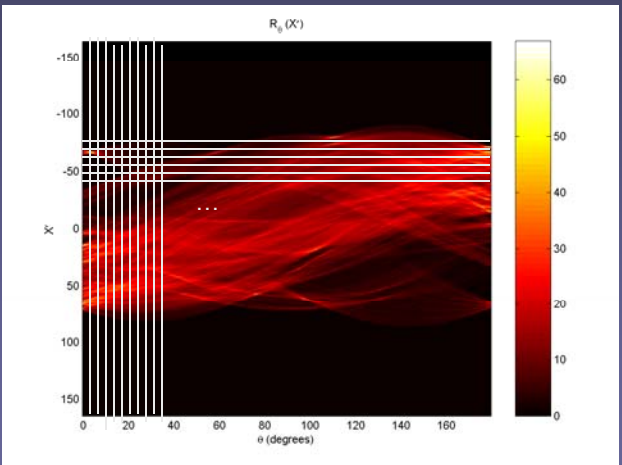
Finding Lines Using the Hough Transform

Strong local peaks correspond to lines.



Finding Lines Using the Hough Transform

Resolution Issues



Bucket Selection

- How to select bucket size?

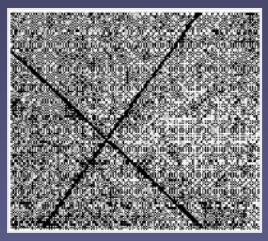
From Szymon Rusinkiewicz, Princeton

Bucket Selection

- How to select bucket size?
  - Too small: poor performance on noisy data
  - Too large: poor accuracy, long running times, possibility of false positives
- Large buckets + verification and refinement
  - Problems distinguishing nearby lines
- Be smarter at selecting buckets
  - Use gradient information to select subset of buckets
  - More sensitive to noise

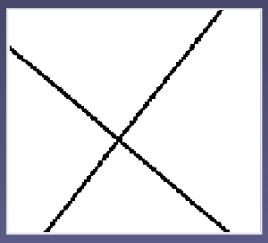
From Szymon Rusinkiewicz, Princeton

Hough Transform: Results



Image

Edge detection



Hough Transform

Summary Hough Transform

- Smart counting
  - Local evidence for global features
  - Organized in a table
  - Careful with parameterization!
- Problem: Curse of dimensionality
  - Works great for simple features with 3 unknowns
  - Will fail for complex objects
- Problem: Not a local algorithm

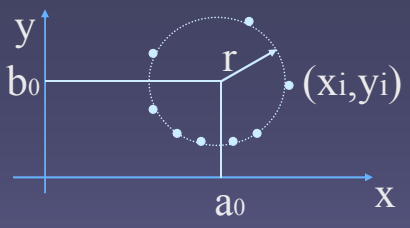
Hough Transform

- What else can be detected using Hough transform?

Hough Transform

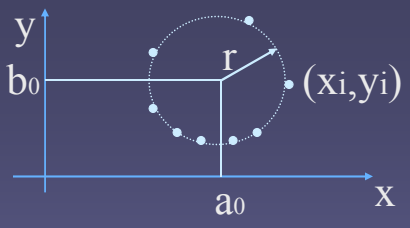
- What else can be detected using Hough transform?
- Anything, but *dimensionality* is key

Finding Circles by Hough Transform



Equation of Circle: $(x_i - a_0)^2 + (y_i - b_0)^2 = r^2$

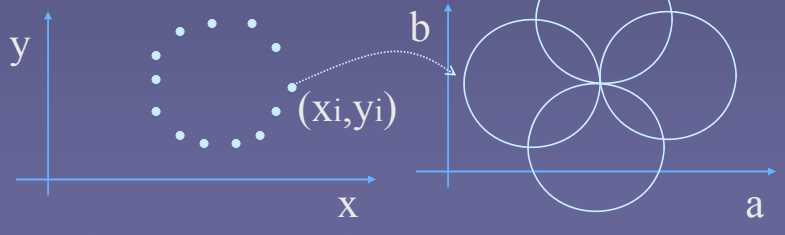
Finding Circles by Hough Transform



Equation of Circle: $(x_i - a_0)^2 + (y_i - b_0)^2 = r^2$

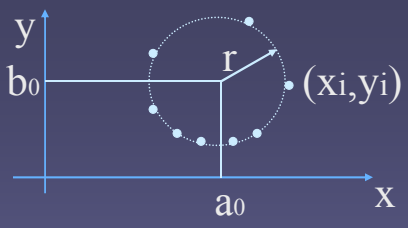
If radius r is known:

Circles!



Accumulator array A(a,b)

Finding Circles by Hough Transform



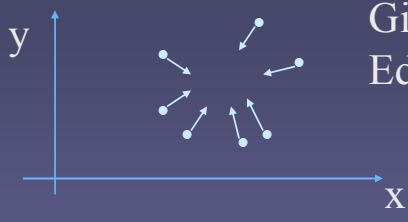
If r is not known
Use accumulator array A(a,b,r)

For each (x_i,y_i) increment A(a,b,r) such that

$$(x_i - a)^2 + (y_i - b)^2 = r^2$$

Using Gradient Information

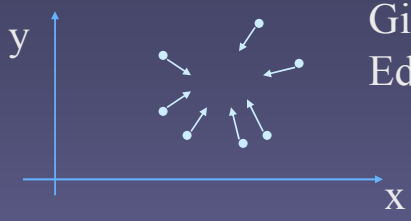
Can save lot of computations!



Given: location (x_i,y_i)
Edge direction φ_i

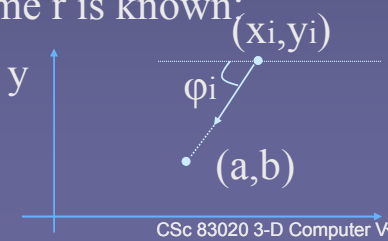
Using Gradient Information

Can save lot of computations!



Given: location (x_i,y_i)
Edge direction φ_i

Assume r is known:



$a=x-r\cos\varphi$
$b=y-r\sin\varphi$

Need to increment only one point in Accumulator Array.