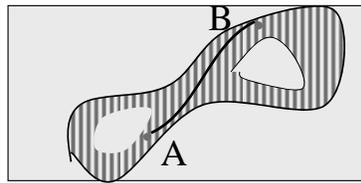


# Multiple Objects

Need to SEGMENT image into separate COMPONENTS (regions).

Connected Component:

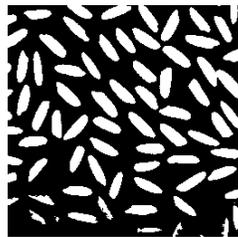
Maximal Set of Connected Points:



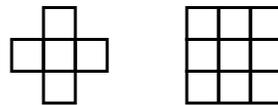
Points A and B are connected: Path exists between A and B along which  $b(x,y)$  is constant.

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# Connected Components



Label all pixels that are connected



4-way connected 8-way connected



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## Region Growing Algorithm (Connected Component Labeling)

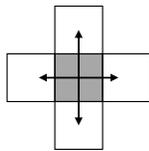
- Start with “seed” point where  $b_{ij}=1$ .
- Assign LABEL to seed point.
- Assign SAME LABEL to its NEIGHBORS ( $b=1$ ).
- Assign SAME LABEL to NEIGHBORS of NEIGHBORS.

Terminates when a component is completely labeled.  
Then pick another UNLABELED seed point.

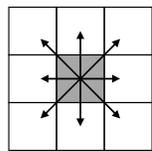
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## What do we mean by NEIGHBORS?

Connectedness



4-Connectedness (4-c)



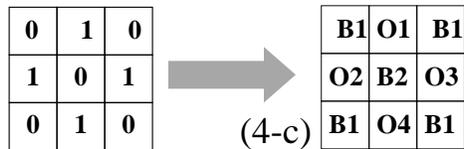
8-Connectedness (8-c)

Neither is perfect!

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# What do we mean by NEIGHBORS?

Jordan's Curve Theorem: Closed curve -> 2 connected regions

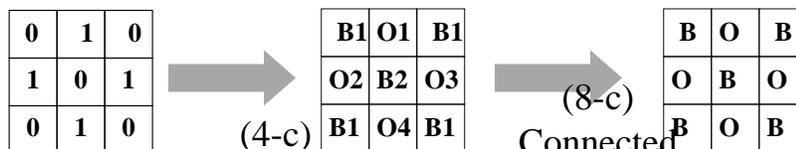


Hole without closed curve!

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# What do we mean by NEIGHBORS?

Jordan's Curve Theorem: Closed curve -> 2 connected regions

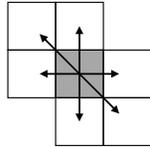


Hole without closed curve!

Connected background  
with closed ring!

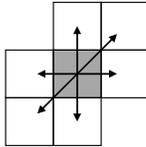
## Solution: Introduce Assymetry

Use:



(a)

or



(b)

Using  
(a)

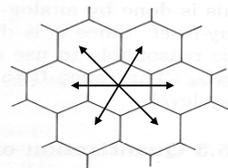
0	1	0
1	0	1
0	1	0



B	O1	B
O2	B	O1
B	O2	B

Two separate line segments.

Hexagonal  
Tesselation



Above assymetry makes  
SQUARE grid like  
HEXAGONAL grid.

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## Sequential Labeling Algorithm

D	B
C	A

Raster Scan

Note: B,C,D are already labeled

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## Sequential Labeling Algorithm

D	B	Raster Scan →
C	A	

Note: B,C,D are already labeled

a. 

X	X
X	0

 Label(A) = background

X	0
---	---

b. 

D	X
X	1

 Label(A) = label(D)

D	X
X	1

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## Sequential Labeling Algorithm

D	B	Raster Scan →
C	A	

Note: B,C,D are already labeled

c. 

0	0
C	1

 Label(A) = label(C)

0	0
C	1

d. 

0	B
0	1

 Label(A) = label(B)

0	B
0	1

d. 

0	B
C	1

 If Label(B) = label(C), then Label(A)=Label(B)=Label(C)

0	B
C	1

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## Sequential Labeling Algorithm

D	B	Raster Scan →
C	A	

Note: B,C,D are already labeled

a. 

X	X
X	0

 Label(A) = background

b. 

D	X
X	1

 Label(A) = label(D)

c. 

0	0
C	1

 Label(A) = label(C)

d. 

0	B
0	1

 Label(A) = label(B)

d. 

0	B
C	1

 If Label(B) = label(C), then Label(A)=Label(B)=Label(C)

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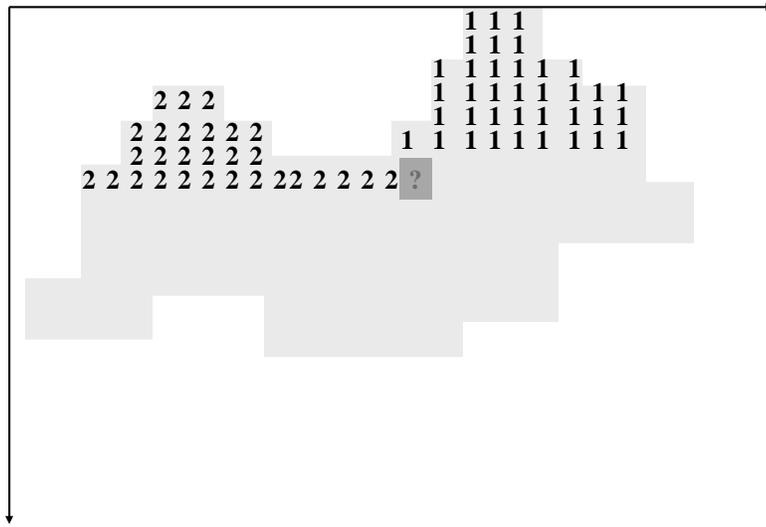
## Sequential Labeling (Cont.)

What if B & C are labeled but label(B)  $\neq$  label(C) ?

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## Sequential Labeling (Cont.)

What if B & C are labeled but label(B)  $\neq$  label(C) ?



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## Sequential Labeling (Cont.)

Solution: Let: Label(A)=Label(B) =2  
& create an EQUIVALENCE TABLE.

Resolve Equivalences in SECOND PASS.

$2 \equiv 1$
$7 \equiv 3,6,4$
...

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