

# Discrete Math

Csci 150 Math for Computer Scientists

Math for Daily life / puzzles

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"Read your hunter email

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## Discrete Math:

- Counting / Combinatorics
- Proofs
- Number Theory (study integers & properties)
- Functions / relations / sets
- Graph theory

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### Example: Birthday Paradox

- Established by Counting
- Proofs: Can you prove that we have infinitely many primes?
- Number Theory

# Two games

## Game 1:

Pick an integer  $x > 0$

-  $x$  is even:  $x \leftarrow x/2$

-  $x$  is odd:  $x \leftarrow 3x + 1$

- Repeat

Ex: 10, 5, 16, 8, 4, 2, 1

## Game 2

Example: 4 integers.

(2, 3, 4, 5)

(1, 1, 1, 3)

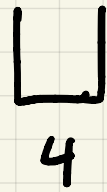
(0, 0, 2, 2)

(0, 2, 0, 2)

(2, 2, 2, 2)

(0, 0, 0, 0)

Puzzle:



$7x - 4y$   
↑      ↑  
Co-prime

Sequences:

Example: Fibonacci

0, 1, 1, 2, 3, 5, 8, 13, ...  
└──────────┘

Recurrences  
└──────────┘  
Def. technique

/ Induction  
└──────────┘  
Proof technique

$$F_n = F_{n-1} + F_{n-2}$$

• Sums :  $1 + 2 + 3 + 4 + 5 + \dots + n = \frac{n(n+1)}{2}$

Example:  $n=1$  : 1

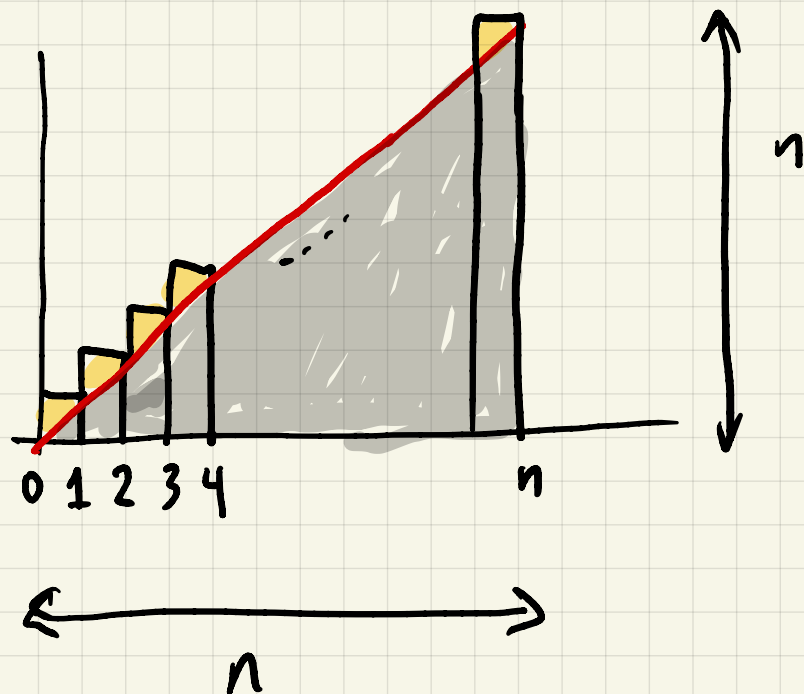
$n=2$  : 3

$n=3$  : 6

$n=4$  : 10

⋮

Geometric Interpretation:



Area of grey triangle:  $\frac{n^2}{2}$

Area of small triangle:  $\frac{1 \times 1}{2} = \frac{1}{2}$

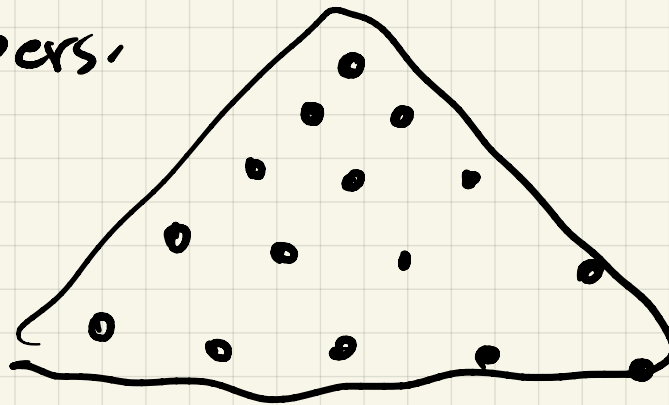
Total:  $\frac{n^2}{2} + n \times \frac{1}{2} = \frac{n(n+1)}{2}$

$$T_n = 1 + 2 + \dots + n$$

$$T_1 = 1, T_2 = 3, T_3 = 6, T_4 = 10, \dots$$

$$T_n = T_{n-1} + n : \text{Recurrence}$$

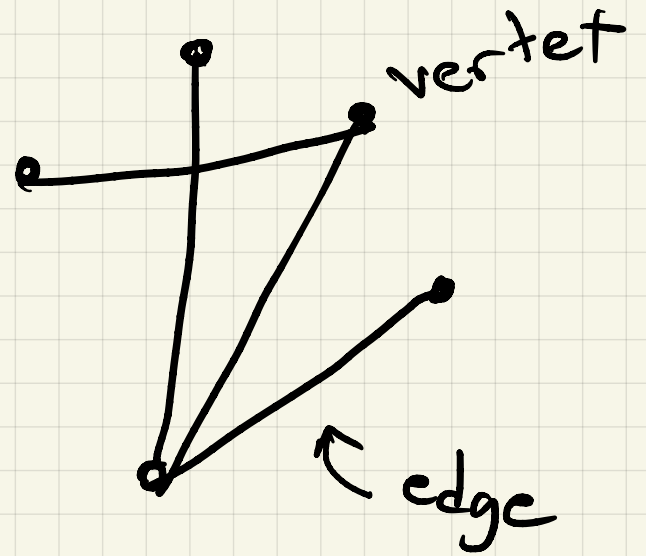
Triangular Numbers.



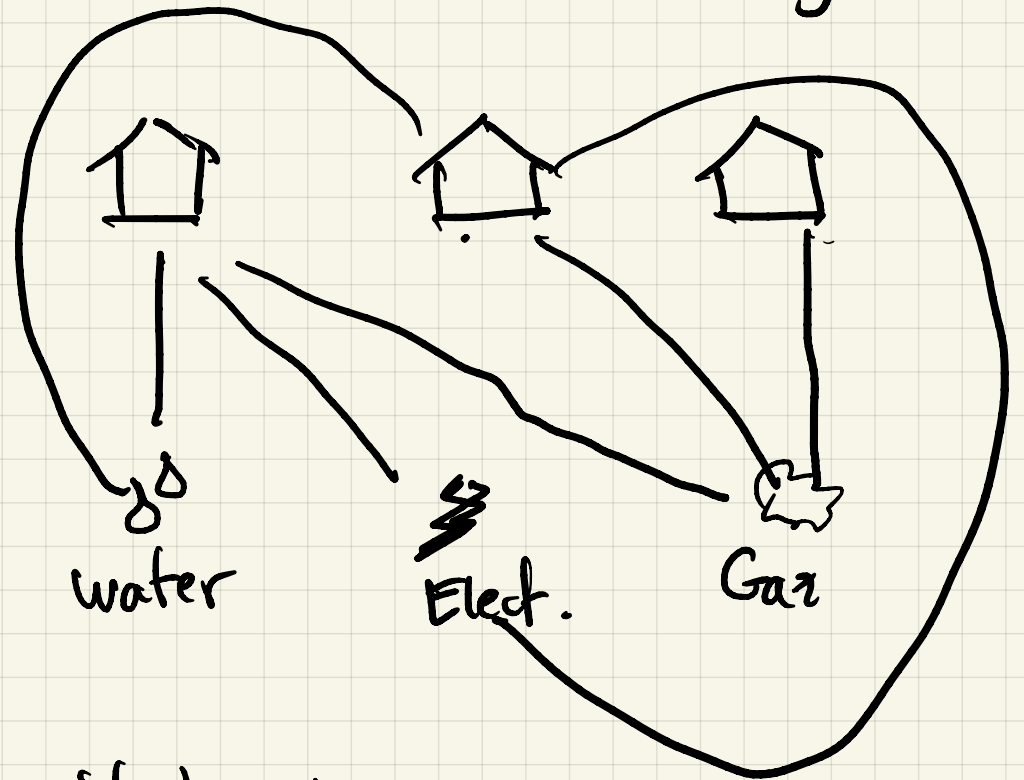
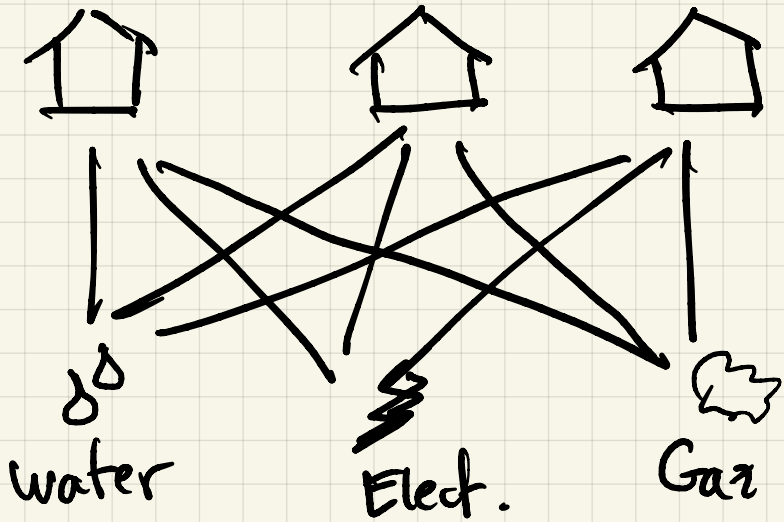
$T_5$

Graphs:

people:



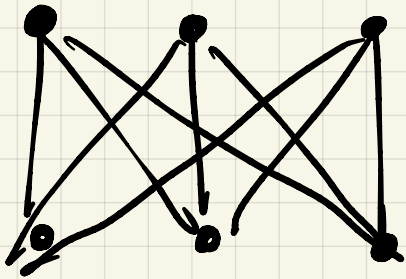
Nasty Neighbors



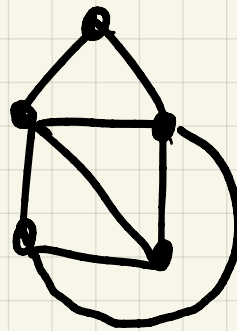
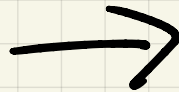
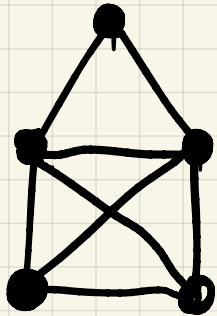
Can't be done without overlap

# Planar Graph

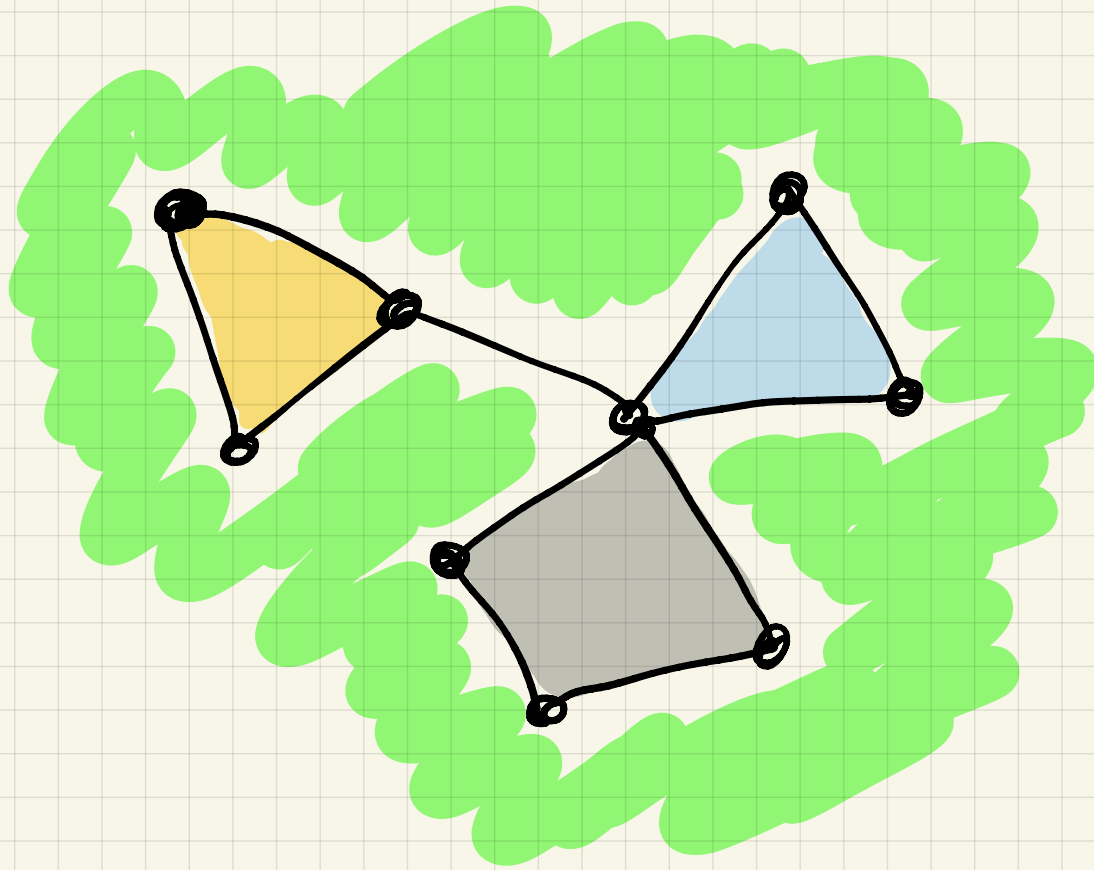
Graph that you can draw in the plane without overlap.



Not planar





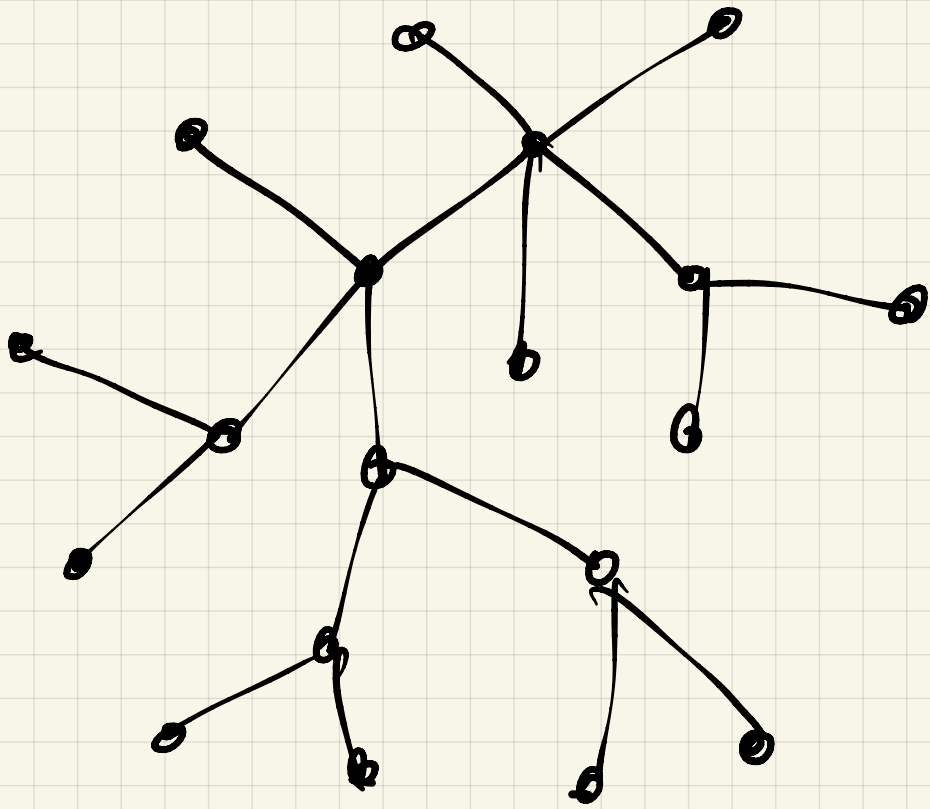


$$V = 9$$

$$e = 11$$

$$f = 4$$

Euler's :  $v - e + f = 2$   
Formula



$$v = e - 1$$

$$1 + 2 + 3 + \dots + n = \frac{n(n+1)}{2}$$

$$1 \times 2 \times 3 \times \dots \times n = n!$$

" Factorial of n "

" n Factorial "

" n! "

$$1! = 1$$

$$2! = 1 \times 2 = 2$$

$$3! = 1 \times 2 \times 3 = 6$$

$$4! = 1 \times 2 \times 3 \times 4 = 24$$

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